Spatio-temporal Analysis of Forest Fires in Portugal ¹

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Abstract: In the last decade, forest fires have become one of the worst natural disasters in Portugal, causing great forest devastation, leading to both economic and environmental losses and putting at risk populations and the livelihoods of the forest itself. In this paper we present Bayesian hierarchical models to analyze spatio-temporal fire data on the proportion of burned area in Portugal, by municipalities and over three decades. Mixture of distributions was employed to model jointly the proportion of area burned and the excess of no burned area for early years. For getting estimates of the model parameters, we used Monte Carlo Markov chain methods.

Keywords: Forest fires, spatio-temporal data, Bayesian hierarchical models.

1 Introduction

According to the National Forestry Authority (Direcção Geral dos Recursos Florestais), Portugal has the largest number of fires among five Mediterranean countries (Portugal, Spain, France, Italy and Greece), being important to look for spatiotemporal patterns of fires e.g. modeling the proportion of burned area. As the proportion of burned area (Y) is a continuous variable and restricted to the interval (0, 1), we can model it by assuming naturally a beta distribution (Ferrari and Cribari-Neto, 2004) or Gaussian distribution and a Skew-Normal (Azzalini and Dalla Valle, 1996) distributions after a logit transformation, i.e. $\log(Y/(1-Y))$. In addition, we can use Bayesian hierarchical models to take into account spatially correlated random effects (Silva et al., 2008) and excess zeros in the proportion of burnt area by municipalities and years (Amaral-Turkman et al., 2010). Our aim is to present a spatio-temporal analysis of forest fires in mainland Portugal, by 278 municipalities between 1980 and 2006, from a Bayesian point-of-view and using Monte Carlo Markov chain (MCMC) methods to obtain estimates of the parameters of interest.

¹This work is partially supported by FCT.

2 Materials and Methods

Let Y_{it} the proportion of burned area in municipality i and year t, $i=1,\ldots,n$, $t=1,\ldots,T$. Assume Y_{it} or $\log(Y_{it}/(1-Y_{it}))$ has a probability distribution with mean μ_{it} and variance σ^2 . Silva et al. (2008) suggest that μ_{it} can be expressed by $\mu_{it}=\alpha+S_0(t)+S_i(t)+\phi_i$, where $S_0(t)$ can represent a nonlinear temporal effect, $S_i(t)$ is the temporal effect by region i and ϕ_i a random effect of the spatial variation associated with region i. If $\phi_i=b_i+h_i$, component h_i represents the unstructured spatial random effect with Gaussian priori distribution $(h_i\sim N(0,\sigma_h^2\equiv\frac{1}{\tau_h}))$, and b_i the spatially correlated random effect with priori distribution, $p(b_i|\tau_b=\frac{1}{\sigma_b^2})$, chosen in terms of a conditional autoregressive model (CAR) (Besag et al., 1981), i.e., $b_i \mid \mathbf{b}_{-i}, \sigma_b^2 \sim N(\bar{b}_i, \sigma_b^2/m_i)$, where \bar{b}_i is the mean of the random effects related to the "neighbors" of the region i, m_i the number of adjacent regions to region i and σ_b^2 the variance component.

Upon the occurrence of zeros, the distribution of the proportion of area burned (Y_{it}) is considered a mixture of distributions with probability function $f(y_{it})$, denoting $f_1(y_{it}) = f(y_{it}|y_{it} \neq 0)$, $i = 1, \ldots, n$, $t = 1, \ldots, T$. Define V_{it} as a Bernoulli random variable such that, $V_{it} = 0$, with probability p_{it_0} , and 1, with probability $p_{it_1} \equiv 1 - p_{it_0}$, where p_{it_0} represents the probability of non-burned area in the region i in the year t. V_{it} indicates the existence of the burnt area in the region i in the year t. Thus, $f(y_{it}) = f_1(y_{it})^{V_{it}} (1 - p_{it_0})^{V_{it}} p_{it_0}^{1-V_{it}}$. The probability of no burned area in the region i at time t is modeled as, $\log(\frac{p_{it_0}}{1-p_{it_0}}) = \beta_0 + \beta_1 t + \psi_i$, where ψ_i is a CAR model. We use assigned highly dispersed but proper priors. In fact, one typically assumes independent normal prior for the regression coefficients. For the variance component hyperparameters, one usually assigns an inverse gamma prior, e.g., $\sigma^2 \sim IG(r_1, s_1)$, $\sigma_b^2 \sim (r_2, s_2)$, $\sigma_h^2 \sim IG(r_3, s_3)$ and $\sigma_\psi^2 \sim IG(r_4, s_4)$ with kernel density given for $x^{-(r+1)}exp(-s/x)$, x > 0. Consequently, we can construct the related joint posteriori distribution and use MCMC methods because the corresponding marginal posteriors are not easy to get explicitly. Notice that these methods are implemented e.g. in WinBUGS (Spiegelhalter et al., 2007).

3 Results and Concluding remarks

Based on the models in Section 2, we analyze the proportion Y_{it} of burnt area due to forest fires in 278 municipalities (mainland Portugal) and over 27 years (1980-2006). Data were collected by Portuguese National Forestry Authority. Three scenarios were considered for the data modeling:

- A) Gaussian probability model: $logit(Y) \sim N(\mu, \sigma^2)$;
- B) Skew-normal model: $logit(Y) \sim SN(\mu, \sigma^2, \lambda)$, where λ is a shape parameter;
- C) Beta model: $Y \sim Beta(a, b)$, with $E[Y] = \mu$, $Var(Y) = \frac{\mu(1-\mu)}{\gamma+1}$ and $\gamma = a+b$.

By using MCMC methods via WinBUGS, we used 15,000 iterations for all fitted models, taking every 10th iteration of the simulated sequence, after 5000 iterations of burn-in. In Table 1, one can be observed some fitted models and, based on the Deviance Information Criterion (DIC), the selected model is model M_4 . Note that $S_0(t) = \eta_t$, in model M_4 , represents a second order random walk. For selected model

Model		p_D	DIC $(\times 10^6)$
$M_1(A)$	$\mu_{it} = \beta_0 + \beta_1 t + \phi_i t + b_i + h_i$	521	150.150
	$logit(p_{it}) = \delta_0 + \delta_1 t + a_i$		
$M_2(B)$	$\mu_{it} = \beta_0 + \beta_i t + \phi_i t + b_i + h_i$	509	150.150
	$logit(p_{it}) = \delta_0 + \delta_1 t + a_i$		
$M_3(C)$	$logit(\mu_{it}) = \beta_0 + \beta_1 t + \phi_i t + b_i + h_i$	581	149.996
	$logit(p_{it}) = \delta_0 + \delta_1 t + a_i$		
$M_4(C)$	$logit(\mu_{it}) = \beta_0 + \eta_t + b_i$	411	149.995
	$logit(p_{it}) = \delta_0 + \delta_1 t + a_i$		

Table 1: Model selection based on DIC

 (M_4) , the posteriori mean, standard deviation (s.d.) and 95% higgest posterior density (HPD) credible Intervals (CI) of some parameters of interest are in Table 2. Based on model M_4 , the spatio-temporal risks of burned area, defined here by $exp(\eta_t+b_i)$ for municipality i, were used to produce maps in 1985, 1994 and 2001 (Figure 1), as well as maps for spatial risks $exp(b_i)$ and $exp(a_i)$ (Figure 2).

parameter	mean	s.d.	95% CI
δ_1	-0.169	0.007	(-0.183, -0.156)
γ	24.82	0.449	(24.02, 25.69)
σ_b^2	0.334	0.051	(0.237, 0.437)
σ_{η}^2	3.357	0.508	(2.424, 4.379)
σ_a^2	0.194	0.060	(0.098, 0.313)
p_{it_0}	0.143	0.003	(0.137, 0.150)

Table 2: Estimates of the model parameters (M_4)

The spatio-temporal analysis of the burned area proportion in 278 municipalities of mainland Portugal between 1980 and 2006 reveals an increasing trend in the proportion of burned area, whereas the number of municipalities without burned area trend to decrease. The space-time models studied here have smoothed estimates used in the production of maps that are useful in the interpretation of spatio-temporal data. This analysis of the Portuguese forest fires may isolate trends in small areas of administrative knowledge for promoting an appropriate policy interventions to reduce that national catastrophe.

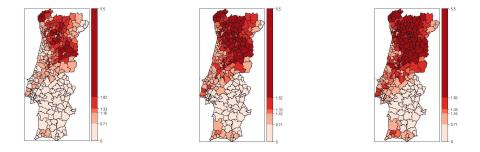


Figure 1: Spatio-temporal risks in 1985 (left), 1994 (middle) and 2001 (right)



Figure 2: Spatial risk maps - $\exp(b_i)$ (left) and $\exp(a_i)$ (right)

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