

1 **Comparative analysis of fixed and sun tracking low power PV systems considering energy**
2 **consumption**

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Abstract - Photovoltaic technology allows to directly convert solar energy into electrical energy with clear advantages: no environmental impact during operation, reliability and durability of the systems, reduced operating costs and maintenance, ability to both supply remote customers and simply connect to the electrical network. This paper evaluates the performance of two photovoltaic systems: one fixed and one equipped with a sun tracker. The objective of this research is to analyze the increase of daily produced energy by using the sun tracking system. The analysis accounts also the energy consumption of the sun tracker. An analytical approach is proposed. To validate the results through experimental tests, two alternative low power PV systems were built. Each system consists of a PV source, a MPPT (Maximum Power Point Tracker) power converter and a 12 V- 40 Ah electrochemical battery, which is used as electric load.. The sun tracker system evidenced an important growth of power production during morning and evening.

Keywords: photovoltaic system, sun tracking, lab prototype, energy analysis

52 Nomenclature and Abbreviations

STC	Standard Test Conditions
NOCT	Nominal operative cell temperature
I_{ph}	current generated by the incidence of light [A]
I_0	reverse saturation current [A]
R_{ph}	shunt equivalent resistance [Ω]
R_s	series equivalent resistance [Ω]
A_i	diode ideality constant
V_T	equivalent voltage, which depends on the temperature [V]
I_{SC}	short circuit current [A]
I_{MP}	maximum power current [A]
V_{OC}	open circuit voltage [V]
V_{MP}	maximum power voltage [V]
MPP	Maximum Power Point
P_{out}	module power output [W]
G	Global solar irradiation onto the plane of the module [W/m ²]
A	module area [m ²]
m	mass of the rigid body
a, b	sizes of the rectangular rigid body
i_o	moment of inertia with respect to an axis passing through the centre of the mass
r	distance between the two parallel axes
E_{rot}	rotational kinetic energy
ω	angular velocity [rad/s]
E_{source}	electrical energy supplied by the external source
η_{motor} , η_{gear}	efficiencies of the electrical machine and of the mechanical system.

1. Introduction

The growing trend in environment protection has determined the introduction of Distributed Generation (DG) interconnected to the existing power systems. The DGs can be interconnected at the point of consumption or to the distribution grids, creating smart grids and micro-grids with economic and social benefits for utilities and customers. In the field of renewable sources used for DG in smart grids, especially at distribution network level, one of the focuses is on PV systems [1]–[4]. The PV systems, converting solar radiation into electrical energy, are pollution-free. Even although their actual cost is still high compared to alternative technologies, the advantages related to PV application are promoting them for massive diffusion. During the period 2005-2013, 550 000 new PV plants were installed in Italy. The PV source's efficiency is related to the ratio among the output electric power and the solar radiation incident on panels. The increase of PV efficiencies is carried on worldwide by many researches to better make use of the sun solar radiation, incident on PV panel. To maximize the PV system output power for any environmental conditions, both PV technology and system's control are studied in detail. The efficiency of the electric generator depends primarily on the PV technology; commercially Si-panels (i.e. monocrystalline- or twin-Si) present the highest values of 17-18%.

In any PV system, the PV source is equipped with a Maximum Power Point Tracker (MPPT) converter. The MPPT makes possible the PV to operate at its instantaneous maximum power point; alternative MPPT strategies are widely applied. Moreover, the overall efficiency of any solar source could be increased by equipping the PV unit with a sun-tracking system. Indeed, the efficiency of any PV electric generator is optimized when the panel surface is aligned with the direction of sunrays (i.e. the amount of “direct” radiation is maximized). Therefore, a solar tracking system can increase the efficiency of the PV panel by adjusting it to be always pointed toward the sun. The appropriate control of the sun tracking system can allow that the system will result in an optimal solar energy collector [5]. Hence, an increased daily and yearly power production will can be achieved. Even although the use of a sun tracker is expensive and increases the complexity of the

overall system, its use can become cost-effective in many cases, as consequence of providing more output energy throughout years [4].

The optimal angle for a solar energy system depends both on site latitude and the final purpose for which the PV it is to be used [6], [7]. Commercially tracking systems are available as either a single-axis or a dual-axis design. The single-axis tracker follows the sun apparent east-to-west movement across the sky, while the dual-axis tracker, in addition to the east–west tracking, controls the solar collector to follow the Sun changing tilt angle [4].

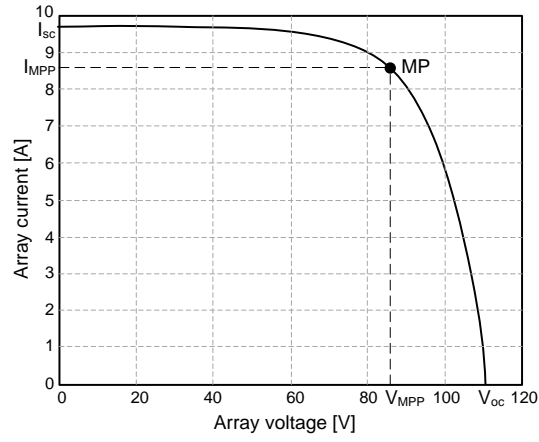
In the last years, design methods for solar tracking systems have been worldwide proposed [8]–[14]. From the analysis, sensing of sun light, providing initial position of the solar panel, control unit design, efficiency assessment, motorization of the tracker are the major challenges of solar tracking systems. Previous studies compared the efficiencies of electricity generated by a fixed and a sun-tracking array. The fixed array are tilted by a fixed angle such that the PV array uses as much as possible the sun radiation at the determined geographical location. The array equipped with sun tracking system adjusts the tilt angle such that to point the sun during its daily movement.

This paper investigates a sun tracker system for PV application. The objective of the research is to highlight the improvement in daily output energy by using the sun tracker. Using two prototypes, experimental tests were carried out during several environmental conditions. The conducted analysis investigates the PV power production, as well as the sun tracker energy consumption. Hence, the impact of the auxiliary internal energy consumption on the amount of total produced energy can be assessed.

2. Photovoltaic electric source

Any PV source is an array of cells (connected in series or parallel) converting the incident solar radiation into electrical energy [14]. The PV array characteristic curve represents a non-linear I-V curve depending on operating voltage, temperature and irradiance. Fig. 1 shows a typical solar array

104 curve at Standard Test Conditions (STC) (irradiance of 1000 W/m², cell temperature of 25°C, air
 105 mass of 1.5).

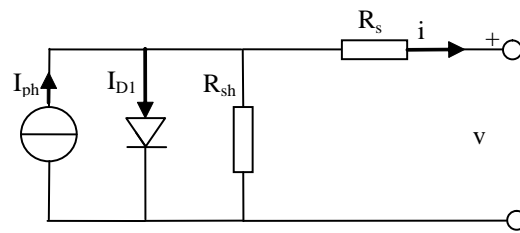


106

107 Fig. 1. Photovoltaic (PV) array characteristic curve.

108 In Fig. 1, the short-circuit current I_{sc} and open-circuit voltage V_{oc} identify the operative limits on
 109 the axes. The area of the largest rectangle that can be fitted under the curve represents the maximum
 110 power that the electrical source produces.

111 Several electric circuits and analytical models can represent the PV electrical behavior [5]. In
 112 many applications, the equivalent circuit illustrated in Fig. 2 is used. The current-voltage
 113 characteristic is given by:



114

115 Fig. 2. Photovoltaic (PV) equivalent circuit.

$$I = I_{ph} - \frac{v + R_s \cdot I}{R_{sh}} - I_{D1} \quad (1)$$

$$I_{D1} = I_0 \cdot \left[\exp\left(\frac{v + R_s \cdot I}{A_i \cdot V_T}\right) - 1 \right]$$

116 where I and v are the PV terminal current and voltage, I_{ph} represents the photo-current [A]; I_0
 117 represents the reverse current [A]; R_{sh} represents the shunt equivalent resistance [Ω]; R_s represents
 118 the series equivalent resistance [Ω]; A_i is the diode quality factor; V_T represents the equivalent
 119 voltage, which depends on the temperature [V].

120 The PV module efficiency η is the ratio between the power delivered by the module and the
 121 irradiation power per area multiplied by the active area of the module [15]:

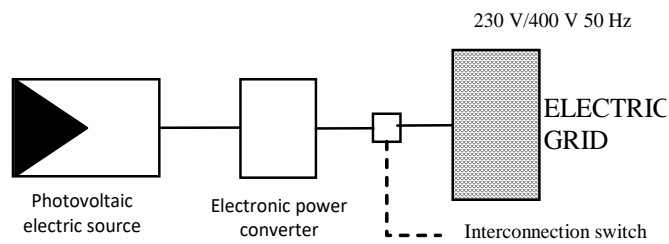
$$\eta = \frac{P_{out}}{G \cdot A} \quad (2)$$

122 The efficiency is maximized when the source operates on the instantaneous maximum power
 123 point (MPP). By analyzing (2) it can be observed that PV output power can be increased by
 124 improving the accuracy of MPPT algorithm, or/and by maximizing the amount of solar irradiance
 125 useful for the conversion into electric energy.

126

127 3. PV power systems with sun tracking

128 The PV systems, generating a DC power, are connected to the 50 Hz mains through an electronic
 129 power converter. Fig. 3 shows the electrical power system configuration.



130

131 Fig. 3. PV electrical power system configuration

132

133 The power converter maximizes the energy production in any atmospheric conditions by
 134 controlling the PV output power. This converter implements the Maximum Power Point Tracker
 135 (MPPT), which controls the source efficiency according to the environmental conditions. Therefore,

136 it is usually possible to find applications with one or two stages of power converters. In the first
137 case, the converter is operating to control the MPPT, and balancing source and load/grid
138 requirements. In the second case, the former power electronic stage acts as MPPT, whereas the later
139 follows grid requirements.

140 As the solar irradiation consists of direct, and indirect or diffuse light (i.e. the light which has
141 been scattered by dust and water particles in the atmosphere), and PV sources primary use the direct
142 irradiation, the behavior of any PV source can be improved by acting on the amount of direct light
143 that falls onto the conversion area. Thus, the PV design practices may also include the use of sun
144 tracking systems.

145 A sun tracker is an electro-mechanical system used for orienting the PV source in the direction of
146 the sun [9, 10]. A sun-tracking mechanism increases the amount of solar energy that can be
147 converted by the source, consequently resulting in a higher annual output power [16].

148 On the market there are available sun tracking systems, with single-axis or dual-axis design
149 [16]-[19]. The single-axis tracker follows the east-to-west sun's movement across the sky, while the
150 dual-axis tracker, in addition to east-west tracking, tilts the PV module to follow the sun's changing
151 altitude angle. Sun tracker controllers can be open-loop or closed-loop. Open-loop controllers are
152 algorithm-based and determine the desired position using an imposed algorithm of solar irradiation
153 geometry model, without using feedback. They are simpler and cheaper than the closed-loop ones,
154 but do not control the output of the processes. Consequently, they cannot correct any errors or
155 compensate for disturbances in the system positions [10]. Closed-loop types are sensor-based. The
156 controller receives as input the feedback of measured state variables. Sensors detect relevant
157 parameters induced by the sun and regulate the output yield by the controller. When the weather is
158 suddenly changing, due to permanent position changes, it is worth to verify if the closed-loop sun
159 tracker consumes more energy as gains.

160

161

4. Test systems

Two PV electrical power systems of the same peak power are used as test system. Fig. 4 shows the schematic representation of the test systems, while Fig. 5 illustrates the developed lab prototypes. One system consists of a PV panel fastened to a fixed metallic support, the other consists of a PV panel fastened to a support equipped with a single-axis sun tracker. In this case, the metallic support is made in such a way as to rotate around the axis of the east-west. Both structures are realized by a tilt inclination of 30° . Each system consists of a PV source (with characteristic data reported in Table 1), a MPPT power converter and a 12 V- 40 Ah electrochemical battery, which is used as electric load (Fig. 4).

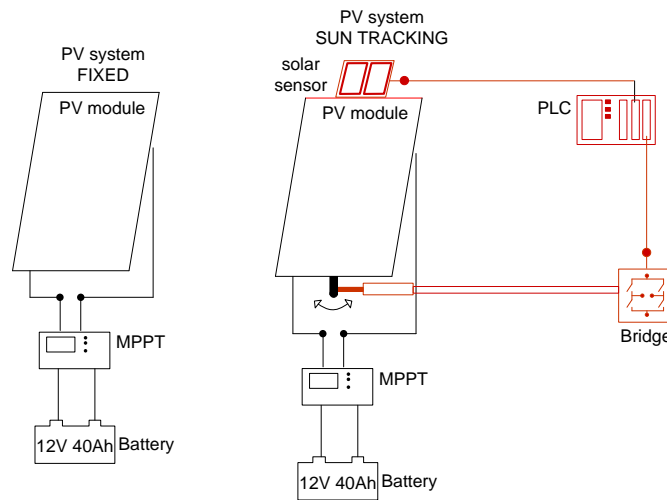


Fig. 4. Fixed and sun-tracking PV power test systems.



Fig. 5. Sun-tracking and fixed PV test systems.

176 The tracker consists of a mechatronic system composed of mechanics, electric drive, and
177 information technology. The PV panel is able to rotate on its ~~axis~~ axis by an angle of 120°. For
178 realizing a simple and low cost tracking system, the tracker is a closed-loop system using two
179 photo-sensors. The tracker, sensible to the sun position, is using two photo sensors [14], in-built
180 with the PV source. The sensors are able to determine the optimal position of the PV collector,
181 when the illumination of the two photo-sensors becomes equal and balanced. A PLC receives the
182 input control signal and commands a DC electric machine to move the PV module in such direction.

183 The PV characteristic data at STC (i.e. initial values) and at Nominal Operating Cell
184 Temperature-NOCT (i.e. nominal values) are reported in Table 1. The NOCT is defined as the
185 temperature reached by open circuited cells in a panel under irradiance on cell surface of 800 W/m²,
186 air temperature of 20°C, wind velocity of 1 m/s, and open back side mounting.

187 Table 1. PV panel data @ STC and NOCT

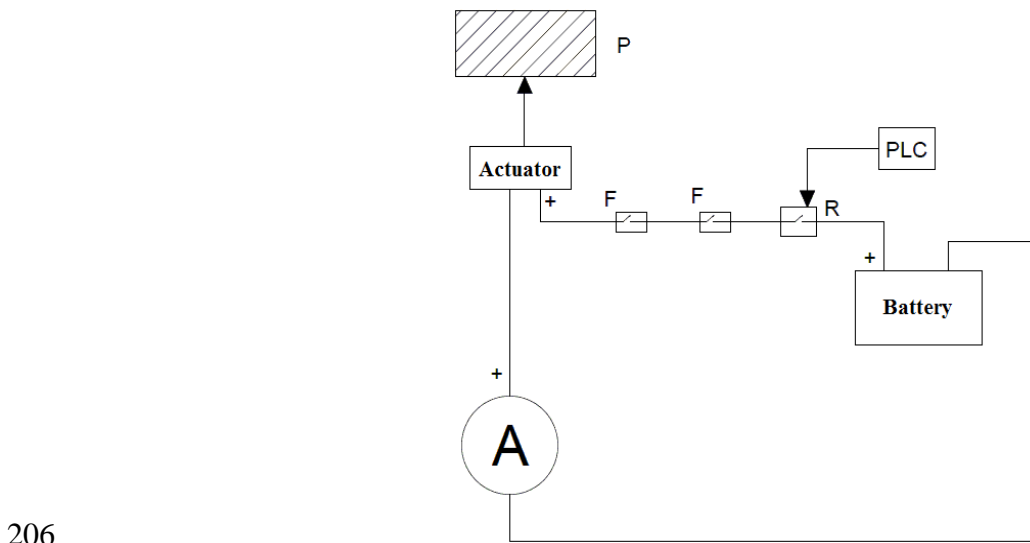
Characteristic Data		
Module	Initial Value (STC)	Nominal Value (NOCT)
Peak power	142.4 W _p	121 W _p
Open-circuit voltage V _{OC}	60.2 V	59.2 V
Short circuit current I _{SC}	3.43 A	3.35 A
Maximum power voltage V _{PM}	48.2 V	45 V
Maximum power current I _{PM}	2.96 A	2.69 A
Normal Operating Cell Temperature (NOCT)		44 °C
Temperature Coefficient (P _{max})	-0.30 mV/°C	-0.30 mV/°C
Temperature Coefficient (V _{oc})	+ 0.07 %/°C	+ 0.07 %/°C
Temperature Coefficient (I _{sc})	-0.24 %/°C	-0.24 %/°C

188

189 The built prototype system is moved by a DC motor powered by a 12 V battery, as shown in Fig. 4.
 190 The actuator (i.e. the DC geared motor) is able to move the installation for a full rotation east-west
 191 of 120°. A relay bridge controls the DC motor to rotate clockwise and counter-clockwise. A PLC
 192 manages the bridge relay status, based on data from the sensors and according to the two limit
 193 switches. These two switches disable the rotation control when the east and west terminal positions
 194 are reached.

195 The energy used by an electrical drive for sun tracking depends on the mass of the PV installation
 196 that is moved, as well as on the efficiency of DC motor and gear transmission box (i.e. the actuator).
 197 Considering that for this type of application, the angular speed is low, the ideal energy amount to
 198 move the PV installation is relatively small (see formulation reported in appendix). However, small
 199 efficiencies in DC geared-motor and mechanical frictions can strongly influence the real amount of
 200 used energy.

201 For determining the energy consumed by the electrical drive during the tests, a series of
 202 experiments imposing the full rotation of the installation were conducted. Fig.6 shows the block
 203 diagram of the circuit and the measuring system. In Fig. 6, *A* indicates the electrical ampermeter, *P*
 204 indicates the panel and the structure that supports the panel, *F* indicates the “limit” switches for the
 205 application, and *R* indicates the bridge relay controlled by the PLC.



206
 207 Fig. 6. Measuring circuit of the implemented sun-tracking PV power system

208 The measurement system is able to record the voltage and the current with a sampling time of
 209 0.5 s. Table 2 reports the results of conducted tests. Fig. 7 illustrates the variation of current
 210 function the rotation angle, during two performed experimental tests.

211 Table 2. Obtained values of electrical current measured during the experimental tests

Time [s]	I ₁ [A]	I ₂ [A]	Rotation Angle [°]
0	0	0	0
0.5	1.7	1.64	12
1	1.41	1.37	24
1.5	1.14	1.1	36
2	0.94	0.88	48
2.5	0.71	0.65	60
3	0.5	0.43	72
3.5	0.66	0.64	84
4	0.86	0.82	96
4.5	0.12	0.06	108
5	0	0	120

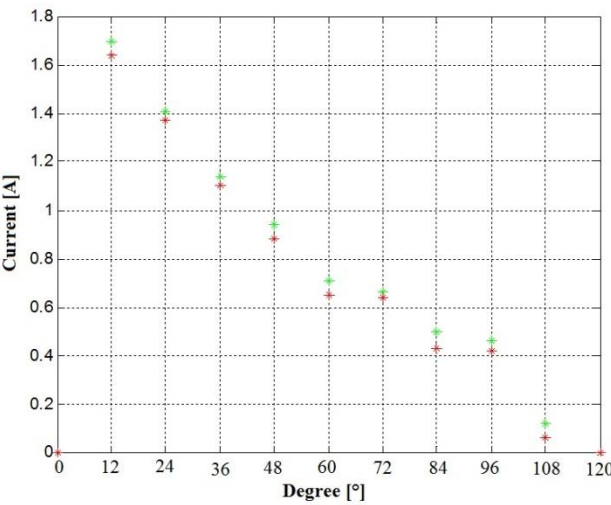


Fig. 7. The typical trend of the currents observed during the experimental campaign.

215 The experimental test results reveal that:

216 1) the electric drive is able to complete a full rotation east-west in about 5 s;

217 2) the angular speed can be assessed as constant during the rotation, with an average value of
218 12° every 0.5 s;

219 3) the electric power is maximum at start-up and decreases to minimal values with time.

220 As the electrical drive is supplied by a 12 V battery source, the average energy consumed by the
221 electrical drive for a full 120° rotation can be estimated as about 50 Ws, with a power peak value of
222 about 20 W during the first instants of the rotation. This energy represents the average value that the
223 system must use at sunset to move the installation to the initial east position, in order to be ready for
224 the next day.

225

226 **5. Experimental results**

227 To evaluate the performances of the two PV systems, these were operated simultaneously. The
228 values of electrical current and voltage were acquired with a 15 min sample rate on an online
229 computer. The systems were exposed to east and the output powers were calculated according to the
230 obtained data.

231 The investigations were conducted during the months of May and June 2014, for an amount of 30
232 days. Measurements were performed in the day interval 8,00-19,00. For each system, the
233 instantaneous output power and daily produced energy were recorded. Based on the results and
234 weather conditions, the monitoring days were classified according to three classes:

235 - case A: clear sky (15 days);

236 - case B: partially clear sky (9 days);

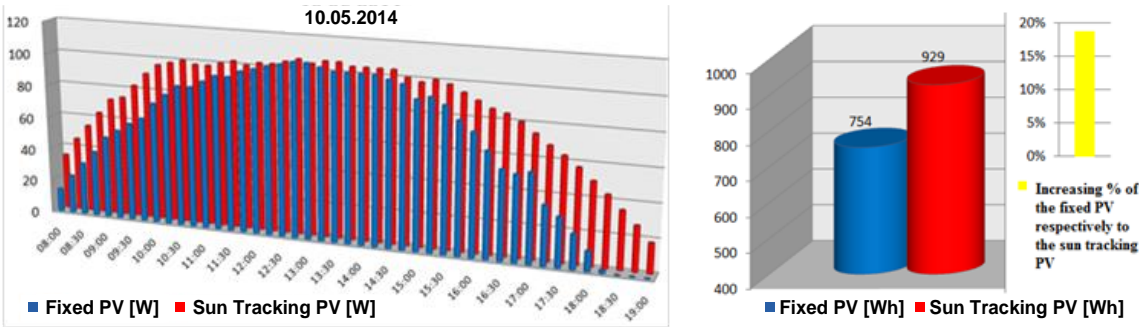
237 - case C: cloudy sky (6 days).

238 Fig. 8 shows different outputs in specific days of May, in particular May 10, 18 and 25. In this
239 way it is possible to observe the distribution of the output power in different irradiation conditions:
240 "clear sky", "partially clear sky", "cloudy sky". The measured output powers of the PV systems are

241 compared as a function of the time, whereas on the right the amounts of produced energy were
 242 compared.

243

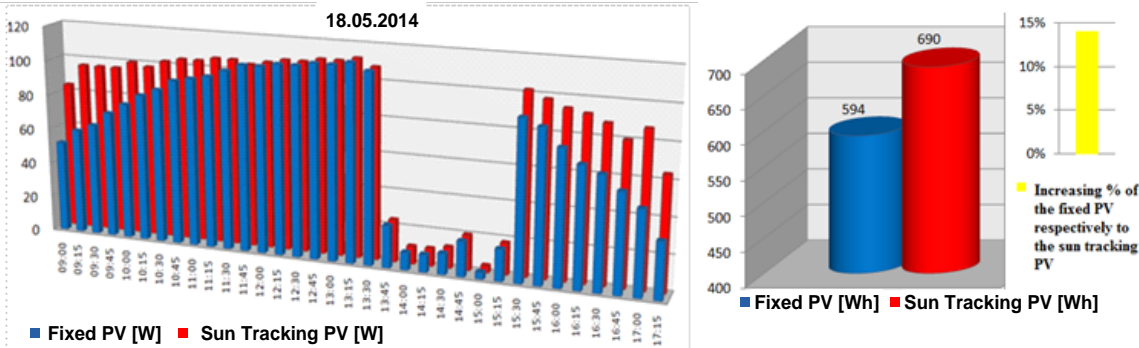
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(A)

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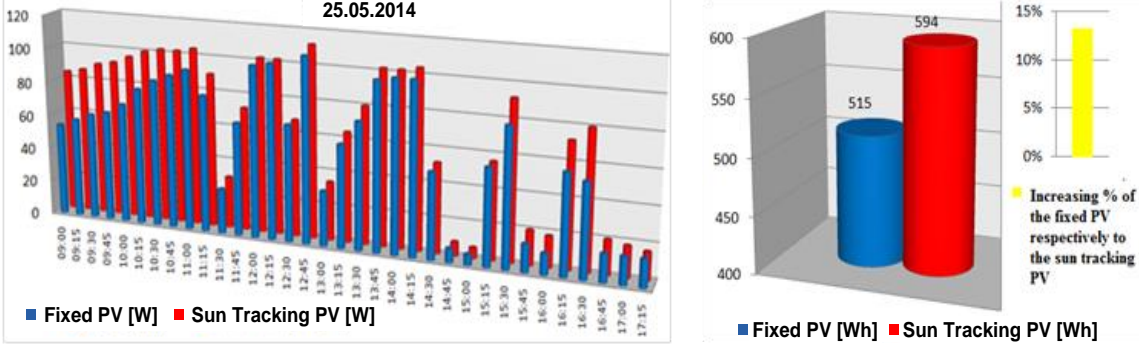
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(B)

247

248



(C)

249 Fig. 8. Output power evaluated in different conditions (a) clear sky (b) partially clear sky and (c)
 250 cloudy sky.

251

252 In case A (i.e. "clear sky" conditions), the power varies regularly during the day, reaching its
 253 maximum at the middle of the monitoring period, as shown in Fig. 8 (a). The first and last hours of

the day highlights the effectiveness of the sun tracker. During these hours, the improvement of the output power among the two PV systems is, as expected, extremely relevant. In case B (i.e. "partially clear sky conditions"), the action of the sun tracker is also highlighted at the beginning and ending of the day, as illustrated in Fig. 8 (b). Whereas the weather condition makes the action of the sun tracker does not relevant in case C (i.e. cloudy sky conditions), when the energy spent to move the panel cannot be compensated by the improvement of power, as shown in Fig. 8 (c).

In terms of daily average energy, the sun tracker system is able to improve the total produced energy of the PV system. The increase depends on the weather conditions and varies between 12% and 20 %. The growth is maximized during "clear sky" days, when the sun tracker's action improves the performance of the PV source especially during the ending hours of the day.

To assess the real gain in the average produced energy with the PV tracking system, the power losses of the auxiliaries used to move the structure must be considered. The useful energy can be defined as the "net" energy, expressed as the difference between the produced energy and the energy consumed by the sun tracker auxiliaries. The minimal energy consumption can be analyzed by adopting a flexible control strategy and an efficient mechanical solution.

As expected, based on the experimental tests reported in Fig.8, during "clear sky" days the sun tracker produces a discontinuous unidirectional movement of the structure from east-to-west. In case of "partially clear sky" and especially "cloudy sky" days, the movement can result alternative in direction and continuous in time, as consequence of the instantaneous sky varying conditions. In "clear sky" days, it was observed that the solar tracking system is usually active only for few instants, while correcting the position of the panel with respect to the sun for every one hour of duty. Thus, the average value of the daily consumed energy by the test system (i.e. actuator losses) was estimated around 100-200 Ws. Similar results are obtained for different days and weather conditions (warm and cold conditions). The power losses due to moving the structure are small compared to the gained power [20]. Thus, considering the increase of energy used by the solar tracking system (a few percent of the produced energy), it is possible to summarize that the net

energy produced by the solar tracker can be estimated as almost equal to the total energy produced by the system.

6. Conclusions

Maximizing the energy yield of PV systems in order to generate the highest possible return on investment is an ongoing research. The objective of this paper is to compare two alternative photovoltaic systems. One is a fixed, whereas the second one is a PV system equipped with a sun tracker. The sun tracker is able to increase the amount of daily direct radiation incident on the source. The design of the sun tracker was deeply investigated. In particular, indications to estimate the 50 Ws energy consumed by the sun tracker were analyzed in detail. For comparing the performances of the two systems, two PV lab prototypes were built and investigated during a 30 days monitoring campaign. The experimental results highlight the significant increase 12-20 % of the produced energy by using the sun tracker. In addition, the results obtained during "clear sky" days show that any solar tracker must be designed such that to limit the energy consumption caused by small variations of solar irradiation.

Based on the results obtained during "partially clear sky" and "cloudy sky" days, further research to countermeasure the random irradiation variations must be conducted. In this way, the energy consumption associated with unnecessary rotations of PV source can be limited.

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Appendix

The moment of inertia of any rectangular rigid body respect to an axis passing through the centre of the mass, can be expressed as:

$$i_o = m \cdot \left[\frac{(a^2 + b^2)}{12} \right]$$

If the rotation axis does not pass through the centre of the mass, the Huygens–Steiner theorem

357 provides a convenient expression to compute the moment of inertia of a rigid body around an axis z ,
358 which is parallel to the axis passing through the centre of the mass. The moment of inertia i_z with
359 respect to axis z is given by:

$$i_z = i_o + m \cdot r^2$$

360 where r is the distance between the two parallel axes.

361 The energy consumed for rotating any rigid body with respect to an axis passing through the
362 centre of the mass, E_{rot} , is the rotational kinetic energy. For any angular velocity ω , E_{rot} depends on
363 the rotational moment of inertia i_o by:

$$E_{rot} = \frac{1}{2} \cdot i_o \cdot \omega^2$$

364 The energy E_{source} , supplied by the external source to the electrical drive for sun tracking, depends
365 also on the efficiencies of the DC motor and gear transmission box. Therefore, E_{source} can be
366 assessed using:

$$E_{source} = \frac{E_{rot}}{\eta_{motor} \cdot \eta_{gear}}$$

367